

Evidential Force Aggregation

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Abstract - In this paper we develop an evidential force aggregation method intended for classification of evidential intelligence into recognized force structures. We assume that the intelligence has already been partitioned into clusters and use the classification method individually in each cluster. The classification is based on a measure of fitness between template and fused intelligence that makes it possible to handle intelligence reports with multiple nonspecific and uncertain propositions. With this measure we can aggregate on a level-by-level basis, starting from general intelligence to achieve a complete force structure with recognized units on all hierarchical levels.

Keywords: Force aggregation, clustering, classification, Dempster-Shafer theory, template.

1 Introduction

We define force aggregation as a combination of two processes. First, an association of intelligence reports, objects or units (depending on hierarchical level) by a clustering process [1–5] the left column in Figure 1. Secondly, a classification of cluster content through a comparison with templates, the right column in Figure 1. In Figure 1 such clustering and classification is performed on all hierarchical levels, level-by-level to achieve a complete force aggregation of all units.

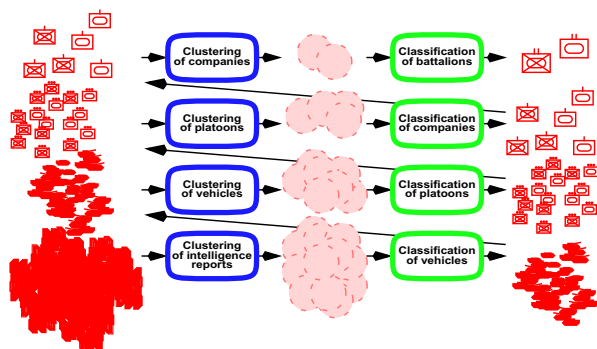


Figure 1: The aggregation process hierarchy.

Evidential force aggregation is force aggregation from uncertain information. The classification in evidential force aggregation is the focus of this paper.

The work described herein is an extension of previous work. In [6] we restricted each intelligence report to carry only one proposition that could be specific or nonspecific regarding object types, i.e., support any subset of all possible types, but was always certain. Here, in this paper, we allow for any number of nonspecific and uncertain propositions in each intelligence report. With this extension we may handle any general intelligence report.

The classification process deals with intelligence reports on a cluster-by-cluster basis. Looking at intelligence in one of the clusters, the classification from intelligence by templates take place in two phases. First, we combine all intelligence reports within the cluster, and secondly, we compare the combined intelligence with all available templates.

In the combination of intelligence a special concern is the representation used. As the reports in general are not reports about the same object or group of objects, we must not use a simple representation dealing only with object type. Instead, we must use a more advanced representation that allow us to keep track of different objects and their possible types. Intelligence reports that actually are referring to the same object or group of objects are precombined, and henceforth viewed as one intelligence report. When this is done, all intelligence reports in the cluster under investigation can be combined, giving us the possibility to investigate the different resulting hypothesis regarding force composition.

When selecting a template for the current cluster we search for a maximum matching between template and fused intelligence. Since intelligence consists of multiple alternative hypothesis with an accompanying uncertainty we must take every hypothesis into account, to its degree of uncertainty, when evaluating a template. As these hypothesis are also nonspecific regarding object type, i.e., they refer to a subset of all possible types instead of to a single type, we cannot expect a perfect matching for each type of object in the template. Instead, we look for possibility of a matching between intelligence and template, i.e., the

absence of conflicts in numbers between what the intelligence propose and what each available template request for all subsets of types. With this measure we can select a template for intelligence with nonspecific propositions.

A few other approaches to force aggregation than the one described here are [7–10].

In Sect. 2 we describe the representation of intelligence and their combination. An example is given in Sect. 2.1. In Sect. 3 we describe the representation of templates and their evaluation and selection through a comparison with intelligence. A continuation of the example is presented in Sect. 3.1. An evidential force aggregation algorithm based on the result of the two previous sections is presented in Sect. 4. Finally, conclusions are drawn (Sect. 5).

2 Intelligence

We will here investigate the representation and combination of all intelligence referring to the same unit. We assume that a number of intelligence reports about different set of objects are available. These reports have already been partitioned into subsets where each subset corresponds to a unit on one hierarchical level higher [2, 3]. Let us hereafter focus on one such subset \mathcal{X}_a and the aggregation of the intelligence in this subset.

Let TY be a set of all possible types of objects $\{TY_x\}$; where TY_x is a type of vehicle or a type of unit depending on which hierarchical level we are at.

Let I_a be a set of any number of intelligence reports in cluster \mathcal{X}_a ,

$$I_a = \{C_a^i\}_i. \quad (1)$$

We use Dempster-Shafer theory [11–16], to represent the uncertainty of all intelligence reports. Each intelligence report focuses on a separate set of objects and is represented by a set of any number of alternative pairs

$$\{(C_a^i \bullet n_j, C_a^i \bullet pt_j)\}_j, \quad (2)$$

i.e., focal elements. Each pair has a possibly nonspecific proposition about possible types

$$C_a^i \bullet pt_j \subseteq TY \quad (3)$$

and a corresponding possibly nonspecific number of such types

$$C_a^i \bullet n_j \subseteq \mathbb{Z}^+, \quad (4)$$

i.e., a subset of $\{1, 2, \dots\}$, where

$$N_{C_a} = \max_{ij} \{\max C_a^i \bullet n_j\} \quad (5)$$

is the maximum number of objects. Each focal element, in the set of Eq. (2), has a basic probability number

$$m_i^{I_a}[(C_a^i \bullet n_j, C_a^i \bullet pt_j)] \quad (6)$$

indicating the uncertainty in each proposition.

If we receive several reports focused on the same object or set of objects they are precombined into C_a^i . Multiple nonalternative propositions about other objects than the $C_a^i \bullet n_j$ objects described as $C_a^i \bullet pt_j$ are handled as additional but separate intelligence reports.

In this situation we have a single frame about the number of objects for each subset of object types X ,

$$\Theta_X = \{(i, X)\}_{i=0}^{N_{C_a}} \quad (7)$$

where $X \subseteq TY$.

In order to be able to handle reports about different objects that should not be combined on the object level, but should be viewed as fragments of a larger unit structure where all fragments are to be combined, we need to refine our representation. Each report is now corresponding to a unique position in a unit structure.

The frame of discernment when fusing reports regarding different sets of objects that should be combined as fragments of a larger unit structure becomes

$$\Theta_{I_a} = \{\langle x_1, x_2, \dots, x_{|I_a|} \rangle\} \quad (8)$$

where

$$x_i = (x_i \bullet n, x_i \bullet pt), \quad (9)$$

is information regarding the i^{th} set of objects with

$$x_i \bullet n \subseteq \{1, \dots, N_{C_a}\}, \quad (10)$$

and

$$x_i \bullet pt \subseteq TY. \quad (11)$$

Thus, we have

$$|\Theta_{I_a}| = (|TY| \cdot N_{C_a})^{|I_a|} \quad (12)$$

The set of all intelligence reports I_a in this representation becomes

$$J_a = \left\{ \left\{ m_i^{J_a}(\langle \theta_1, \dots, \theta_{i-1}, x_i, \theta_{i+1}, \dots, \theta_{|I_a|} \rangle) \right\}_{\{x_i\}} \right\}_{i=1}^{|I_a|} \quad (13)$$

where

$$x_i \in \{(C_a^i \bullet n_j, C_a^i \bullet pt_j)\}_j \quad (14)$$

is one of the propositions of intelligence report number i ; C_a^i .

Let us begin the analysis of all intelligence by combining all mass functions $m_i^{J_a}$ of J_a , $\oplus J_a$.

Resulting from this combination we get

$$m_{\oplus J_a}(\langle x_1, x_2, \dots, x_{|I_a|} \rangle) = \prod_{i=1}^{|I_a|} m_i^{J_a}(\langle \theta_1, \dots, \theta_{i-1}, x_i, \theta_{i+1}, \dots, \theta_{|I_a|} \rangle) \quad (15)$$

the basic probability number for each alternative hypothesis.

As we are also interested in the types of objects and their number regardless of their ordering, we sum up all contributions regarding the same type.

We let

$$m_{\oplus J_a}^{I_a}[(X \bullet n_j, X \bullet pt_j)] = \sum_{\langle x_1, x_2, \dots, x_{|I_a|} \rangle} m_{\oplus J_a}^{J_a}(\langle x_1, x_2, \dots, x_{|I_a|} \rangle) \left| \begin{array}{l} X \bullet n_j = \bigoplus_i x_{i \bullet n} \\ i | x_i, pt = X \bullet pt_j \end{array} \right. \quad (16)$$

where $\bigoplus_i x_{i \bullet n}$ is the direct sum of all $x_{i \bullet n}$'s, not to be confused with Dempster's rule \oplus , as in $m_{\oplus J_a}^{I_a}$. The result is a set of elements, each element the sum of one element from every set $x_{i \bullet n}$, i.e.,

$$\bigoplus_i x_{i \bullet n} = \left\{ \sum_i y_i \mid y_i \in x_{i \bullet n} \right\}, \quad (17)$$

e.g., the direct sum $\{1, 2\} \oplus \{2, 3\} = \{1+2, 1+3, 2+2, 2+3\} = \{3, 4, 4, 5\} = \{3, 4, 5\}$. This gives us information about different propositions in the initial representation with Θ_X as frame of discernment. The result of Eq. (16) will not be used in the selection process of finding a template with maximal fitness for the intelligence in \mathcal{X}_a . However, it is a result in itself that may be communicated for other purposes.

2.1 An example

Let us observe an example with two intelligence reports and four possible vehicles. The first report has an uncertainty about whether the observation reported upon was of two main battle tanks (*MBT*) or two armored personnel carriers (*APC*), but with a strong preference for the first. It is initially represented as

$$\begin{aligned} m_1^{I_a}[\{\{2\}, \{MBT\}\}] &= 0.5, \\ m_1^{I_a}[\{\{2\}, \{MBT, APC\}\}] &= 0.3, \\ m_1^{I_a}(\Theta) &= 0.2, \end{aligned} \quad (18)$$

stating that we have a 0.5 basic probability in favor of two *MBTs*, a 0.3 basic probability in favor of two vehicles that are either *MBTs* or *APCs*.

The second report is uncertain both about the number of vehicles and the type of the vehicle observed;

$$\begin{aligned} m_2^{I_a}[\{\{1, 2\}, \{MBT, APC\}\}] &= 0.6, \\ m_2^{I_a}(\Theta) &= 0.4, \end{aligned} \quad (19)$$

stating that we have a 0.6 basic probability of one to two vehicles that are *MBTs* or *APCs*.

Representing these reports in the frame of Eq. (8), we obtain

$$\begin{aligned} m_1^{J_a}[\langle \{2\}, \{MBT\} \rangle, \theta_2] &= 0.5, \\ m_1^{J_a}[\langle \{2\}, \{MBT, APC\} \rangle, \theta_2] &= 0.3, \\ m_1^{J_a}[\langle \theta_1, \theta_2 \rangle] &= 0.2. \end{aligned} \quad (20)$$

and

$$\begin{aligned} m_2^{J_a}[\langle \theta_1, \{1, 2\}, \{MBT, APC\} \rangle] &= 0.6, \\ m_2^{J_a}[\langle \theta_1, \theta_2 \rangle] &= 0.4. \end{aligned} \quad (21)$$

Here, we have

$$J_a = \left\{ m_1^{J_a}, m_2^{J_a} \right\}. \quad (22)$$

We combine the two mass functions of J_a , Eqs. (20) and (21), to obtain

$$\begin{aligned} m_{\oplus J_a}(\langle \{2\}, \{MBT\} \rangle, \langle \{1, 2\}, \{MBT, APC\} \rangle) &= 0.3, \\ m_{\oplus J_a}(\langle \{2\}, \{MBT\} \rangle, \theta_2) &= 0.2, \\ m_{\oplus J_a}(\langle \{2\}, \{MBT, APC\} \rangle, \langle \{1, 2\}, \{MBT, APC\} \rangle) &= 0.18, \\ m_{\oplus J_a}(\langle \{2\}, \{MBT, APC\} \rangle, \theta_2) &= 0.12, \\ m_{\oplus J_a}(\langle \theta_1, \{1, 2\}, \{MBT, APC\} \rangle) &= 0.12, \\ m_{\oplus J_a}(\langle \theta_1, \theta_2 \rangle) &= 0.08. \end{aligned} \quad (23)$$

using Eq. (15). This result will be used in the next section to select a template with maximum fitness towards the intelligence.

Temporarily, we return to the previous representation using Θ_X as the frame of discernment in order to obtain a basic probability assignment for each supported subset of all types of objects TY .

We sum up the contribution of Eq. (23) using Eq. (16), to receive

$$\begin{aligned} m_{\oplus J_a}^{I_a}[\{\{2\}, \{MBT\}\}] &= 0.3 + 0.2 = 0.5, \\ m_{\oplus J_a}^{I_a}[\{\{0\}, \{MBT\}\}] &= 0.18 + 0.12 + 0.12 + 0.08 \\ &= 0.5, \\ m_{\oplus J_a}^{I_a}[\{\{3, 4\}, \{MBT, APC\}\}] &= 0.18, \\ m_{\oplus J_a}^{I_a}[\{\{2\}, \{MBT, APC\}\}] &= 0.12, \\ m_{\oplus J_a}^{I_a}[\langle \{1, 2\}, \{MBT, APC\} \rangle] &= 0.3 + 0.12 = 0.42, \\ m_{\oplus J_a}^{I_a}[\langle \{0\}, \{MBT, APC\} \rangle] &= 0.2 + 0.08 = 0.28. \end{aligned} \quad (24)$$

This summarizes the support for each supported subset of all types TY . Note, that the first two sum to 1.0, and the four last sum to 1.0 as these are two different assignments.

3 Templates

Comparing templates having specific propositions that are certain in what they are requesting with intelligence propositions that are not only uncertain but may also be nonspecific in what they are supporting can be a difficult task. The idea we use to handle this problem is to compare a candidate template with intelligence from the perspective of each and every subset of all possible types of objects TY .

In doing this we investigate how much support a subset of TY receives both directly and indirectly from intelligence and template, respectively. The support for a subset of TY is summed up from all propositions that are equal to or itself a subset of this subset of TY . This is similar to the calculation of belief from basic probability numbers in Dempster-Shafer theory, except that we are not summing up basic probability numbers but natural numbers representing the number of objects of the proposed types.

For example, from the perspective of $\{MBT, APC\}$ a template proposition of “four $MBTs$ ” lend indirect support to $\{MBT, APC\}$ since $\{MBT\}$ is a subset of $\{MBT, APC\}$, and intelligence proposing “two $MBTs$ or $APCs$ ” lend direct support to the subset. With the summed up numbers being four and two, respectively, we have a mismatch between template and intelligence from the perspective of $\{MBT, APC\}$. We use this method to rank all templates based on a fitness measure of template to intelligence matching taking all subsets of TY into account.

By using the result obtained by Eq. (15) from the combination of all mass functions in J_a , we compare different templates in order to find a template with maximum fitness towards the set of intelligence reports.

Let T be a set of all available templates $\{T_i\}$. Each template is represented by any number of slots S_i^j where $S_i^j \cdot pt \in TY$ is a possible type from the set TY and $S_i^j \cdot n$ is the number of that type i T_i .

Based on the combination of all intelligence reports, Eq. (15), we evaluate all templates of $\{T_i\}$.

As we have several different alternative propositions in the intelligence regarding the type of objects and their corresponding number of objects, we need to compare each potential template with these alternatives and let each proposition influence the evaluation. For each template we find a measure of fitness between the template and each proposition in the intelligence, separately,

$$\pi_{\langle x_1, x_2, \dots, x_{|I_d|} \rangle}(T_i). \quad (25)$$

We then make a linear combination where each measure of fitness is weighted by the basic probability number of that proposition,

$$m_{\oplus J_a}(\langle x_1, x_2, \dots, x_{|I_d|} \rangle). \quad (26)$$

We get

$$\begin{aligned} \pi_{\oplus J_a}(T_i) &= \sum_{\langle x_1, x_2, \dots, x_{|I_d|} \rangle} m_{\oplus J_a}(\langle x_1, x_2, \dots, x_{|I_d|} \rangle) \pi_{\langle x_1, x_2, \dots, x_{|I_d|} \rangle}(T_i) \end{aligned} \quad (27)$$

as the measure of fitness of T_i towards all intelligence in \mathcal{X}_a . This is the measure by which we rank all templates and make our selection of template.

In [6] we evaluated all templates T_i by comparing each template against a set of intelligence reports with a single certain and specific proposition. This is here extended to handle intelligence reports with multiple uncertain and nonspecific propositions. We have

$$\begin{aligned} \pi_{\langle x_1, x_2, \dots, x_{|I_d|} \rangle}(T_i) &= \frac{1}{2} [\pi_{\langle x_1, x_2, \dots, x_{|I_d|} \rangle}^1(T_i) + \pi_{\langle x_1, x_2, \dots, x_{|I_d|} \rangle}^2(T_i)] \end{aligned} \quad (28)$$

as a measure of fitness for template T_i towards one of these multiple propositions $\langle x_1, x_2, \dots, x_{|I_d|} \rangle$, where

$$\pi_{\langle x_1, x_2, \dots, x_{|I_d|} \rangle}^1(T_i) = \min_j [\pi_{\langle x_1, x_2, \dots, x_{|I_d|} \rangle}^3(T_i | S_a^j \cdot pt)], \quad (29)$$

with $S_a^j \cdot pt \subseteq TY$, is a measure of fitness looking for a worst matching between T_i and this proposition for all different subsets of all types TY .

Here,

$$\begin{aligned} \pi_{\langle x_1, x_2, \dots, x_{|I_d|} \rangle}^3(T_i | S_a^j \cdot pt) &= \begin{cases} \max_{n \in SC_a(S_a^j \cdot pt)} \left\{ \min \left[\frac{n}{ST_i(S_a^j \cdot pt)}, \frac{ST_i(S_a^j \cdot pt)}{n} \right] \right\}, & ST_i(S_a^j \cdot pt) > 0 \\ 1, & ST_i(S_a^j \cdot pt) = 0 \end{cases} \end{aligned} \quad (30)$$

is a measure of fitness for template T_i towards the same propositions $\langle x_1, x_2, \dots, x_{|I_d|} \rangle$ from the perspective of $S_a^j \cdot pt$ only.

The second measure in Eq. (28),

$$\pi_{\langle x_1, x_2, \dots, x_{|I_d|} \rangle}^2(T_i) = \max_{n \in SC_a(TY)} \left\{ \min \left[\frac{n}{ST_i(TY)}, \frac{ST_i(TY)}{n} \right] \right\} \quad (31)$$

is only looking for the correct number of objects in T_i and in proposition $\langle x_1, x_2, \dots, x_{|I_d|} \rangle$ of the intelligence, regardless of object types.

While the first measure $\pi_{\langle x_1, x_2, \dots, x_{|I_d|} \rangle}^1(T_i)$ measures

the fitness of T_i on a type-by-type basis demanding a perfect fit for all types to give a full score, the second measure ignores type entirely, and compare the number of objects of all intelligence in \mathcal{X}_a with the same in the template. While the first measure seems preferable it can be too extreme when considering missing data for same small number $S_i^j \cdot n$ of objects in T_i .

Note that $ST_i(S_a^j \cdot pt) \forall i, j$ in Eq. (30) and $ST_i(TY) \forall i$ in Eq. (31) can be precomputed using Eq. (32) below as they are independent of intelligence.

For each potential template T_i we calculate the number of objects requested by the template from the perspective of subset $X \subseteq TY$ in Eq. (30), (31) as

$$\forall X \subseteq TY. ST_i(X) = \sum_{j | S_i^j \cdot pt \subseteq X \cdot pt} S_i^j \cdot n, \quad (32)$$

and the number of objects supported by proposition $\langle x_1, x_2, \dots, x_{|I_a|} \rangle$ of the intelligence from the perspective of subset $X \subseteq TY$ in Eq. (30), (31) as

$$\forall X \subseteq TY. SC_a(X | \langle x_1, x_2, \dots, x_{|I_a|} \rangle) = \sum_{\substack{i | x_i \in \langle x_1, x_2, \dots, x_{|I_a|} \rangle \\ |x_i \cdot pt \subseteq X \cdot pt}} x_i \cdot n \quad (33)$$

where $\bigoplus_i x_i \cdot n$ is the same direct sum of integer sets as in Eq. (17); each element in the resulting set the addition of one element from every set $x_i \cdot n$.

Here, we assume that $x_i \cdot n = \{0, \dots, N_{C_a}\}$ and not $\{0\}$ when $x_i = \theta_i$. There is after all a difference between having a report that is uncertain about its proposition and being sure there is no object at all. The latter being a very strong statement.

While the fitness measure $\pi_{\bigoplus J_a}(\cdot)$ is used for aggregation from the current hierarchical level, we

also need the basic probability of the highest ranked template for any further aggregation from the next hierarchical level.

We combine the intelligence, Eq. (15), with a basic probability assignment stating that the set of all templates is true,

$$m_T(\{T_i\}) = 1. \quad (34)$$

Each focal element in the resulting combination support a subset of all templates. Through a fitness weighted transformation, these templates will share this support in relation to their fitness towards the corresponding focal element in the intelligence.

We find the basic probability number of a template T_i as

$$m_{\bigoplus J_a}(T_i) = \sum_{\langle x_1, x_2, \dots, x_{|I_a|} \rangle \supseteq T_i} \left\{ m_{\bigoplus J_a}(\langle x_1, x_2, \dots, x_{|I_a|} \rangle) \times \frac{\pi_{\langle x_1, x_2, \dots, x_{|I_a|} \rangle}(T_i)}{\sum_{\langle x_1, x_2, \dots, x_{|I_a|} \rangle \supseteq T_j} \pi_{\langle x_1, x_2, \dots, x_{|I_a|} \rangle}(T_j)} \right\} \quad (35)$$

using Eqs. (15) and (28).

3.1 An example continued

Let us evaluate templates based on a comparison with the result of Eq. (15) (in Eq. (23)). Let us assume we have two templates one with four main battle tanks (*MBTs*) and one with three armored personnel carriers (*APCs*). Our frame of discernment is $\Theta = \{MBT, APC\}$.

Table 1: Number allowed by templates (ST_1, ST_2) and supported by intelligence (SC_a) for different propositions $S_a^j \cdot pt$.

		{MBT}	{APC}	{MBT, APC}
$ST_1(\cdot)$	$\{\{4\}, \{MBT\}\}$	4	0	4
$ST_2(\cdot)$	$\{\{3\}, \{APC\}\}$	0	3	3
$SC_a(\langle \cdot \rangle)$	$\langle \{\{2\}, \{MBT\}\}, \{\{1, 2\}, \{MBT, APC\}\} \rangle$	{2}	{0}	{3, 4}
	$\langle \{\{2\}, \{MBT\}\}, \theta_2 \rangle$	{2}	{0}	$\{2, \dots, N_{C_a}\}$
	$\langle \{\{2\}, \{MBT, APC\}\}, \{\{1, 2\}, \{MBT, APC\}\} \rangle$	{0}	{0}	{3, 4}
	$\langle \{\{2\}, \{MBT, APC\}\}, \theta_2 \rangle$	{0}	{0}	$\{2, \dots, N_{C_a}\}$
	$\langle \theta_1, \{\{1, 2\}, \{MBT, APC\}\} \rangle$	{0}	{0}	$\{1, \dots, N_{C_a}\}$
	$\langle \theta_1, \theta_2 \rangle$	{0}	{0}	$\{0, \dots, N_{C_a}\}$

Table 2: A measure of fitness $\pi_{\langle \cdot \rangle}^3(T_i | \cdot)$ between each template proposition and every proposition in fused intelligence.

	T_1			T_2		
	{MBT}	{APC}	{MBT, APC}	{MBT}	{APC}	{MBT, APC}
$\langle \{\{2\}, \{MBT\}\}, \{\{1, 2\}, \{MBT, APC\}\} \rangle$	2/4	1	4/4	1	0/3	3/3
$\langle \{\{2\}, \{MBT\}\}, \theta_2 \rangle$	2/4	1	4/4	1	0/3	3/3
$\langle \{\{2\}, \{MBT, APC\}\}, \{\{1, 2\}, \{MBT, APC\}\} \rangle$	0/4	1	4/4	1	0/3	3/3
$\langle \{\{2\}, \{MBT, APC\}\}, \theta_2 \rangle$	0/4	1	4/4	1	0/3	3/3
$\langle \theta_1, \{\{1, 2\}, \{MBT, APC\}\} \rangle$	0/4	1	4/4	1	0/3	3/3
$\langle \theta_1, \theta_2 \rangle$	0/4	1	4/4	1	0/3	3/3

We have $T = \{T_1, T_2\}$ where

$$S_1^1 \bullet pt = MBT, \quad S_1^1 \bullet n = 4,$$

and

$$S_2^1 \bullet pt = APC, \quad S_2^1 \bullet n = 3.$$

We also have fused intelligence according to Eq. (23) in Sect. 2.1.

In order to evaluate both templates T_1 and T_2 we calculate $\pi_{\oplus J_a}(T_1)$ and $\pi_{\oplus J_a}(T_2)$ to find their measure of fitness towards the fused intelligence. To calculate these measures we must first calculate the number of objects requested by the templates for each subset of TY using Eq. (32). Using Eq. (33) with the fused intelligence give us the number of objects supported by different propositions in the fused intelligence. In Table 1 we have tabulated the result of $ST_1(\cdot)$ and $ST_2(\cdot)$ for the two templates and $SC_a(\cdot)$ for all propositions in the fused intelligence.

From the result in Table 1 we find $\pi_{\langle \cdot \rangle}^3(T_i | \cdot)$ the measure of fitness of each template towards every $\langle x_1, x_2, \dots, x_{|I_a|} \rangle$ proposition in the intelligence given each subset of TY , in Table 2 using Eq. (30). In the same manner we find $\pi_{\langle \cdot \rangle}^2(\cdot)$, i.e., the same measure of fitness towards all $\langle x_1, x_2, \dots, x_{|I_a|} \rangle$ propositions in the intelligence, but given the set of all types TY (Table 3, using Eq. (31)).

Table 3: $\pi_{\langle \cdot \rangle}^2(T_i)$.

	T_1	T_2
$\langle (\{2\}, \{MBT\}), (\{1, 2\}, \{MBT, APC\}) \rangle$	4/4	3/3
$\langle (\{2\}, \{MBT\}), \theta_2 \rangle$	4/4	3/3
$\langle (\{2\}, \{MBT, APC\}), (\{1, 2\}, \{MBT, APC\}) \rangle$	4/4	3/3
$\langle (\{2\}, \{MBT, APC\}), \theta_2 \rangle$	4/4	3/3
$\langle \theta_1, (\{1, 2\}, \{MBT, APC\}) \rangle$	4/4	3/3
$\langle \theta_1, \theta_2 \rangle$	4/4	3/3

From Table 2 we find the minimum fitness $\pi_{\langle \cdot \rangle}^1(T_i)$ for both templates towards every proposition in the fused intelligence given all subsets of TY (tabulated in Table 4, using Eq. (29)).

Table 4: $\pi_{\langle \cdot \rangle}^1(T_i)$.

	T_1	T_2
$\langle (\{2\}, \{MBT\}), (\{1, 2\}, \{MBT, APC\}) \rangle$	2/4	0/3
$\langle (\{2\}, \{MBT\}), \theta_2 \rangle$	2/4	0/3
$\langle (\{2\}, \{MBT, APC\}), (\{1, 2\}, \{MBT, APC\}) \rangle$	0/4	0/3
$\langle (\{2\}, \{MBT, APC\}), \theta_2 \rangle$	0/4	0/3
$\langle \theta_1, (\{1, 2\}, \{MBT, APC\}) \rangle$	0/4	0/3
$\langle \theta_1, \theta_2 \rangle$	0/4	0/3

Finally, we use Eq. (28) to take $\frac{1}{2}$ of $\pi_{\langle \cdot \rangle}^1(\cdot | T_i)$ and $\pi_{\langle \cdot \rangle}^2(\cdot | T_i)$ for all propositions in Table 3 and Table 4 to get the results in Table 5, $\pi_{\langle \cdot \rangle}(T_i)$.

Table 5: $\pi_{\langle \cdot \rangle}(T_i)$.

	T_1	T_2
$\langle (\{2\}, \{MBT\}), (\{1, 2\}, \{MBT, APC\}) \rangle$	3/4	1/2
$\langle (\{2\}, \{MBT\}), \theta_2 \rangle$	3/4	1/2
$\langle (\{2\}, \{MBT, APC\}), (\{1, 2\}, \{MBT, APC\}) \rangle$	1/2	1/2
$\langle (\{2\}, \{MBT, APC\}), \theta_2 \rangle$	1/2	1/2
$\langle \theta_1, (\{1, 2\}, \{MBT, APC\}) \rangle$	1/2	1/2
$\langle \theta_1, \theta_2 \rangle$	1/2	1/2

Finally, using Eq. (27) to find a linear combination of the measure of fitness in Table 5 (from Eq. (28)) and the basic probability numbers of all propositions in Eq. (23), we obtain measures of fitness for both templates;

$$\begin{aligned} \pi_{\oplus J_a}(T_1) &= 0.3 \frac{3}{4} + 0.2 \frac{3}{4} + 0.18 \frac{1}{2} + 0.12 \frac{1}{2} + 0.12 \frac{1}{2} + 0.08 \frac{1}{2} \\ &= 0.625 \end{aligned}$$

and

$$\begin{aligned} \pi_{\oplus J_a}(T_2) &= 0.3 \frac{1}{2} + 0.2 \frac{1}{2} + 0.18 \frac{1}{2} + 0.12 \frac{1}{2} + 0.12 \frac{1}{2} + 0.08 \frac{1}{2} \\ &= 0.50. \end{aligned}$$

As $\pi_{\oplus J_a}(T_1) > \pi_{\oplus J_a}(T_2)$, template T_1 is the preferred classification of the intelligence in cluster \mathcal{X}_a .

Using Eq. (35) we find the basic probability of T_1 by combining Eq. (23) with $m_T(\{T_1, T_2\}) = 1$. We get

$$\begin{aligned} m_{\oplus J_a}(T_1) &= 0.3 \frac{\frac{3}{4}}{\frac{3}{4}} + 0.2 \frac{\frac{3}{4}}{\frac{3}{4}} + 0.18 \frac{\frac{1}{2}}{\frac{1}{2} + \frac{1}{2}} + 0.12 \frac{\frac{1}{2}}{\frac{1}{2} + \frac{1}{2}} \\ &\quad + 0.12 \frac{\frac{1}{2}}{\frac{1}{2} + \frac{1}{2}} + 0.08 \frac{\frac{1}{2}}{\frac{1}{2} + \frac{1}{2}} = 0.75 \end{aligned}$$

as the first two focal elements intersects to $\{T_1\}$ and the remainder to $\{T_1, T_2\}$.

4 An algorithm for evidential force aggregation

Summarizing the results of Sects. 2 and 3, we find an algorithm for force aggregation from evidential data as follows:

First, combine all intelligence for \mathcal{X}_a as represented in J_a . Secondly, calculate the basic probability number $m_{\oplus J_a}(\langle x_1, x_2, \dots, x_{|I_a|} \rangle)$ for all propositions in the result from $\oplus J_a$, using Eq. (15).

At the same time, calculate the number of objects supported by intelligence $SC_a(\cdot | \langle \cdot \rangle)$ for each subset of all types TY and for each proposition in the intelligence using Eq. (33), and calculate the number of objects requested by each template $ST_i(\cdot)$ for each subset of all types TY and for each proposition in the intelligence, using Eq. (32).

From $SC_a(\cdot | \langle \cdot \rangle)$ and $ST_i(\cdot)$ we may calculate $\pi_{\langle x_1, x_2, \dots, x_{|I_a|} \rangle}(T_i)$ for each template and each proposition in the intelligence by using Eqs. (28), (29), (30), (31).

Finally, calculate a measure of fitness for all templates $\pi_{\oplus J_a}(T_i) \forall i$ based as a linear combination of all $\pi_{\langle x_1, x_2, \dots, x_{|I_a|} \rangle}(T_i)$ using $m_{\oplus J_a}(\langle x_1, x_2, \dots, x_{|I_a|} \rangle)$ and Eq. (27).

The unit that is aggregated from intelligence is T_i for which $\pi_{\oplus J_a}(T_i)$ is maximal, Figure 2.

Finally, we calculate the support of T_i using Eq. (35).

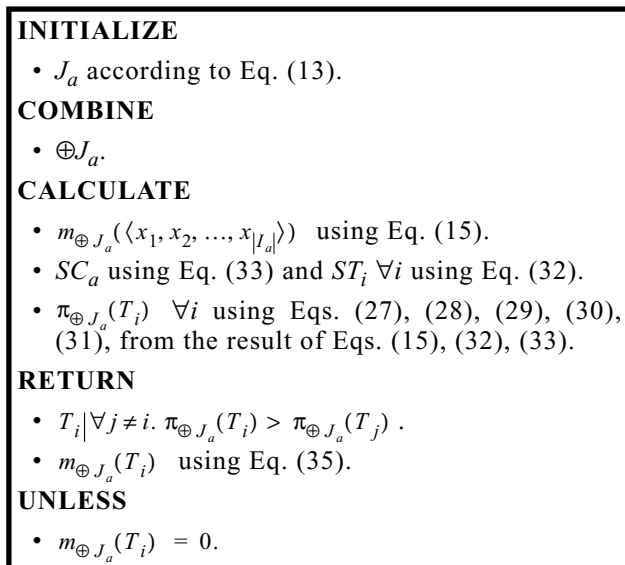


Figure 2: An evidential force aggregation algorithm.

5 Conclusions

The evidential force aggregation method presented makes it possible to aggregate uncertain intelligence reports with multiple uncertain and nonspecific propositions into recognized forces using templates.

This is an extension in two ways compared to earlier methods [6]: (i) it handles intelligence reports that are statistically uncertain, (ii) it handles any number of such propositions. These propositions may continue to be specific or nonspecific in the sense that a proposition may support any subset of all possible object or unit types. With this extension we are able to aggregate general intelligence into units.

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